

Exam of Digital Communications

a.a. 2020-2021

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Exercise #1

A message signal $m(t) = \cos 2000\pi t + 2 \cos 3000\pi t$ modulates the carrier $c(t) = 100 \cos 2\pi f_c t$, where $f_c = 1$ MHz.

- (a) Sketch the spectrum of the lower SSB modulated signal
- (b) Find the complex envelope for the modulated signal

Exercise #2

A signal has a bandwidth of 8kHz. It is sampled, logarithmically compressed and encoded into a PCM format using 8bits per sample. The PCM data is transmitted through an AWGN channel via M-level PAM. Determine the minimum bandwidth required for the transmission when

- (a) $M=4$;
- (b) $M=8$;
- (c) $M=16$.

<https://www.sarthaks.com/2750106/speech-signal-sampled-encoded-format-using-sample-transmitted-through-baseband-channel>

Exercise #3

In an additive white Gaussian noise channel with noise power spectral density of $N_0/2$, two bits are transmitted by

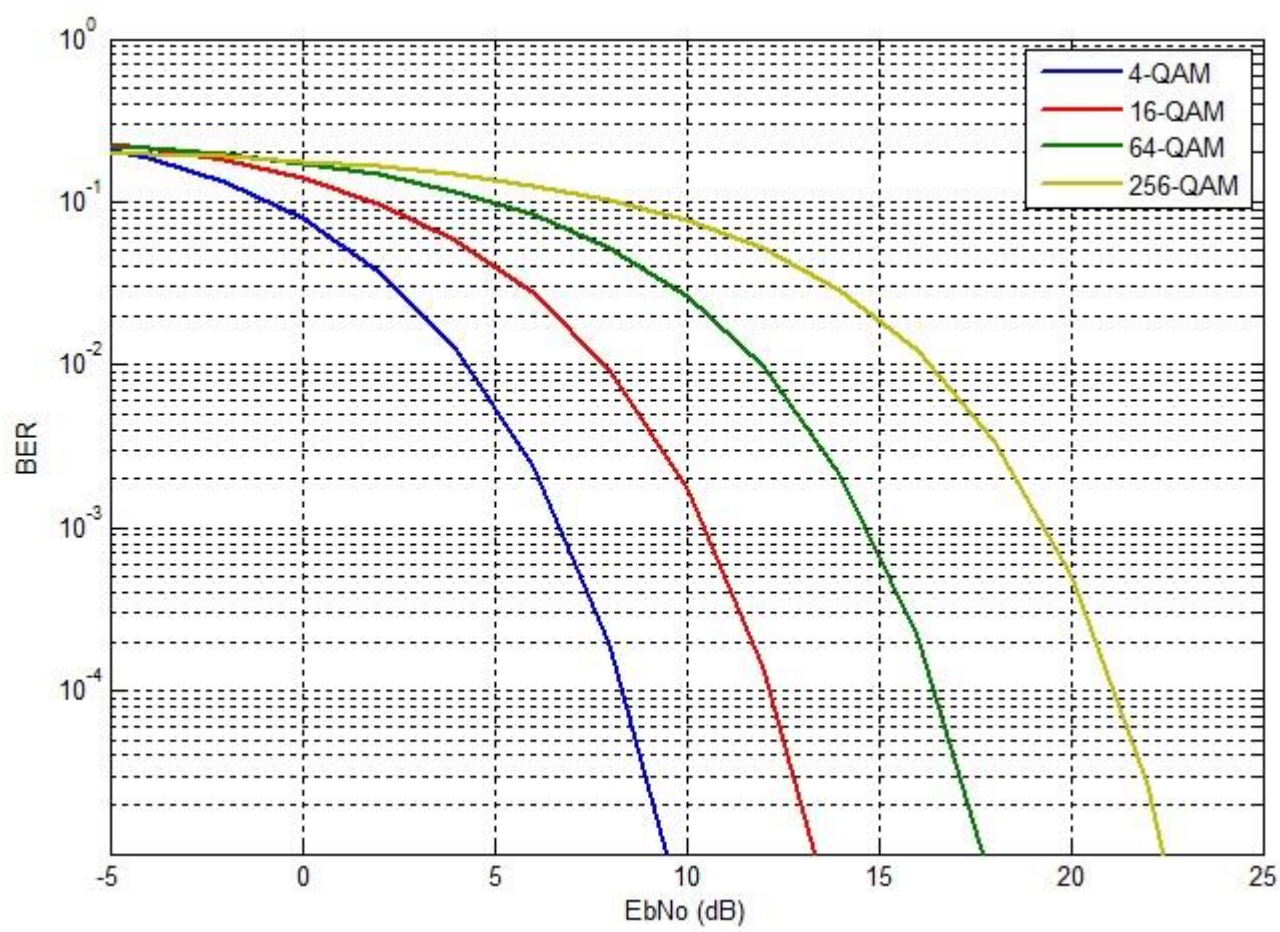
$$s_1(t) = 0$$
$$s_2(t) = \begin{cases} A & 0 \leq t \leq T/2 \\ 0 & T/2 \leq t \leq T \\ 0 & \text{otherwise} \end{cases}$$

The two messages are transmitted with a priori probabilities p and $(1-p)$, respectively.

- (a) Determine the average energy transmitted per bit E_{avb}
- (b) Determine the optimum threshold
- (c) Determine the structure of the optimal receiver (including the detector after the sampler)
- (d) Determine the probability of error in case $p=(1-p)=0.5$.

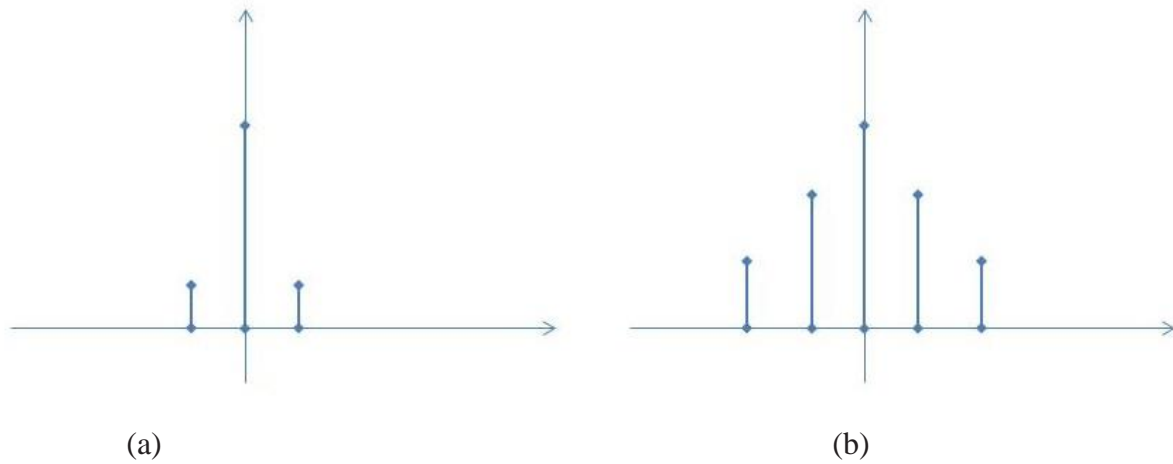
Exercise #4

If the maximum BER is 10^{-4} and SNR is 15dB, which constellations guarantees the maximum bit rate? What is the maximum theoretical bit rate in case with no ISI if the bandwidth available is 3kHz?



Exercise #5

Let us consider two channels that are modeled as linear filter and AWGN. The impulse responses of the two channels are drawn below:



- (a) In which case is more important to use an equalizer at the receiver?
- (b) When the equalizer is not used, how do you expect that the BER curve look like?